**COURSE TITLE:** MATHEMATICAL METHODS IN ECONOMICS III

**COURSE CODE:** ECON 2016

LEVEL:

**SEMESTER:** II

**CREDITS**: 3

**PREREQUISITES:** ECON1004 or PASS in Advanced Level Mathematics or

Pass in CAPE Pure Mathematics

**DEPARTMENT:** ECONOMICS

# **INSTRUCTOR INFORMATION:**

Lecturer and Tutor: Mr. Richard Quarless

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Room Number:

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Tutor Mr. Richard Quarless

Email Address: Room Number: Office Telephone:

## **REQUIRED TEXT**

**Tamara Todorova**: Problems to Accompany Mathematics for Economists, First Edition, John Wiley and Sons, 2011

### HIGHLY RECOMMENDED READING

**K. Sydsaeter and P.J.Hammond**: <u>Mathematics for Economic Analysis</u>, Prentice Hall, New Jersey. Third Edition.2008

#### **COURSE DESCRIPTION:**

This course builds on the foundation provided in the first two level courses in Mathematics and Economics. It will provide Level II Economics students with a wider and deeper exposure to the Calculus of Functions of One Variable as well as Functions of Several Variables and the application of these concepts to the discipline of Economics.

This course is also the last formal Mathematics course for students pursuing a Major or Special in Economics. The concepts in this course are intended to provide you with a solid foundation for the mathematical analysis to be encountered in Microeconomics and Methods of Economic Investigation at the graduate level.

Emphasis will be placed on the understanding and applying mathematical concepts as well as honing problem solving skills rather than mere computational skills, the use of algorithms and the manipulation of formula.

This course is organized into ten (10) units.

## PRE-REQUISITE(S):

ECON 1004 – Mathematics for Economics III ECON 1001 – Introduction to Economics I ECON 1002 – Introduction to Economics II

A Pass in Additional Mathematics, AS Mathematics, or Mathematics at GCE Advanced Level or CAPE will be considered as an alternative prerequisite to ECON 1003.

Students interested in reading this course should refresh their knowledge of

- a. Sets
- b. Matrices
- c. Differential and Integral Calculus
   As set out in the Course Outline for ECON1003 and ECON1004.

#### **PURPOSE OF THE COURSE:**

This course is designed to build on students' understanding of Calculus (as gained at Level I), expose them to mathematical concepts that underpin the mathematical models that will be encountered in the Level II/III and graduate courses in Economics and enhance their problem-solving skills.

# **Goals/Aims**

This course aims to develop the knowledge and problem-solving skills of students reading the Economics Major and Economics Special Programs so that they can:

a. Interpret and use intermediate mathematical data, symbols, terminology and functions

- b. Demonstrate understanding and proficiency in elementary skills in Mathematical Methods for Economics building on the knowledge and skills acquired at Level I
- c. Select the appropriate mix of concept, logic and method of solution required for solving problems in Applied Economics
- d. Apply these mathematical methods to problems in the area of Applied Economics with confidence and accuracy.

## **Advice to Students:**

Courses such as Mathematics require a mix of learning approaches. Students are required to read the lecture materials from one of the course texts prior to the lecture, engage the in-class discussion of that material and supplement these with a second reading of the course text. Such reading and discussion must be followed by work on the tutorial sheets.

Tutorial Sheets are designed to help students flesh out concepts and practice the application of the logic and concepts to a range of problem situations. These are important in this course since they provide the basis for formal practice and assist in reinforcing the concepts introduced in lectures. It is expected that students will also use the texts and recommended references. Every effort should be made to complete each tutorial sheet within the time period indicated on the sheet.

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Students are advised to read through the tutorial sheet to identify the concepts required for its solution prior to revising the concepts so identified; it is only after such revision that you should proceed to attempt the solutions. Some questions in an assignment sheet will be solved in one attempt; others will require more than one attempt. Students are encouraged to adopt co-operative learning approaches (i.e. working with another student or students) to solve the more challenging questions in the tutorial sheet. Always remember that perseverance is a necessary attitude in reading a Mathematics course.

If after the individual effort and the co-operative learning effort, the student feels challenged by a question(s), he/she owes it to himself/herself to seek out the Course Lecturer or Tutor for guidance and assistance.

Under no condition should a student come to a tutorial class unprepared to contribute to the class proceedings. The student's contribution must be the result of his/her efforts invested in the reading of the text/course notes and in solving the tutorial sheet.

Overall students must invest a minimum of <u>seven (7) hours per week</u> apart from lectures, tutorial classes and online quizzes to this course.

Remember to apply yourself consistently from the first week.

## **CONTENT**

The content of the ten units of this course is defined below.

#### Unit 1:

### **Readings: Course Notes**

Revisit of Set Theory, Basic Set Operations, Equality of Sets, De Morgan's Laws. Introduction to the concepts of Boundary Points, Limit Points, Open Sets, Closed Sets, Convex Sets, Concave Sets, Bounded Sets, Compact Sets.

#### Unit 2:

Readings: Course Notes as well as Chaing & Wainwright, Sydsaeter and Hammond, Dowling, Hoffman, Ayres, Parry, or Haussler, Paul and Wood

Revisit of Functions, Inverse Functions, Step Functions, Limit of a Function. Introduction to Monotonic Functions and L'Hopital's Rule.

Applications.

### Unit 3:

Readings: Course Notes as well as Chaing & Wainwright, Sydsaeter and Hammond, Dowling, Hoffman, Ayres, Parry, or Haussler, Paul and Wood

Revisit of Differentiation for functions of one variable.

Introduction to Implicit Differentiation, Logarithmic Differentiation and Elasticity. Applications.

#### Unit 4:

# Readings: Todorova Chapters 4 and 5 as well as Course Notes

Review of Second Order Derivatives for functions of one variable and Global Extreme Points of a function of one variable.

Introduction to Convex and Concave Functions.

Characterization of Points of Inflexion and Maxima and Minima for functions of one variable defined over the entire Real Line or over a closed interval of the Real Line.

The nth Derivative Test.

Curve sketching.

Introduction to Taylor's Theorem.

Applications.

### Unit 5:

# Readings: Todorova Chapter 8 as well as Course Notes

Revisit of Integration for functions of one variable – Indefinite Integrals and Definite Integrals. Double Integrals.

Gini Index and Consumer & Producer Surplus.

Applications.

### Unit 6:

# Readings: Todorova Chapter 9 as well as Course Notes

Introduction to First and Second Order Differential Equations. Solution to first and second order differential equations. Solution of Systems of first or second order differential equations. Applications.

### Unit 7:

# Readings: Todorova Chapter 10 as well as Course Notes

Introduction to First and Second Order Difference Equations. Solution to first and second order difference equations. Solution of Systems of first or second order difference equations. Concept of Stability of a Solution to a difference equation. Applications.

### Unit 8:

# Readings: Todorova Chapters 2 and 3 as well as Course Notes

Introduction to Functions of Several Variables, Partial Derivatives, The Differential, Marginal Analysis, The Chain Rule and Euler's Theorem. Applications.

### Unit 9:

# Readings: Todorova Chapter 6 as well as Course Notes

Unconstrained optimization of functions of several variables utilizing positive definiteness, negative definiteness and indefiniteness.

Applications

### **Unit 10:**

# Readings: Todorova Chapter 7 as well as Course Notes

Constrained Optimization with the objective function and the constraints being functions of several variables. Introduction to Lagrange Multipliers and Kuhn Tucker Conditions.

Applications.

## **UNIT OBJECTIVES:**

**Unit 1**: At the end of this Unit I students must be able to:

- Appropriately and correctly apply De Morgan's Laws
- Identify Boundary Points of Sets
- Manipulate Set Notation
- Classify sets as Open or Closed, Convex or Concave
- Sketch graphs of sets formed from inequalities involving linear, quadratic, exponential and logarithmic functions.

## **Unit 2:** After studying Unit 2 each student must be able to:

- Manipulate function notation
- Create Inverse Functions
- Use L'Hopital's Rule to find limits of functions at a point
- Manipulate Monotonic functions;

# **Unit 3:** By the end of Unit 3, each student must be able to:

- Apply all Rules of Differentiation correctly;
- Apply Implicit differentiation to equations from which the dependent variable cannot be written exclusively as a function of the independent variable;
- Apply Logarithmic Differentiation correctly;
- Perform Marginal Analysis
- Compute Elasticity for a demand function;
- Differentiate between Elastic, Inelastic; and Unit Elastic situations
- Find Extreme Points of a function
- Apply Differentiation the Theory of the Firm

**Unit 4**: By the end of Unit 4, each student must be able to:

- Use Second Order Derivatives to classify functions as Convex or Concave
- Use Second Order Derivatives to classify extreme points of a function
- Compute Higher Order Derivatives
- Sketch functions by identifying important characteristics
- Use Higher Order Derivatives to create series expansion of a function using Taylor's Theorem;

**Unit 5**: By the end of Unit 5, each student must be able to:

- Compute Indefinite Integrals for a range of functions;
- Compute Definite and Double Integrals for a range of functions;
- Compute Gini Index
- Compute Producer & Consumer Surplus;

**Unit 6**: By the end of Unit 6, each student must be able to:

- Classify First Order and Second Order Ordinary Differential Equations;
- Solve First Order and Second Order Ordinary Differential Equations
- Construct Systems of First Order and Second Order Ordinary Differential Equations
- Solve systems of First Order and Second Order Ordinary Differential Equations

**Unit 7**: By the end of Unit 7, each student must be able to:

- Classify First Order and Second Order Difference Equations;
- Solve First Order and Second Order Difference Equations
- Check for stability in the solution of a Difference Equation
- Construct Systems of First Order and Second Order Difference Equations
- Solve systems of First Order and Second Order Ordinary Difference

### **Equations**

**Unit 8**: By the end of Unit 8, each student must be able to:

- Manipulate functions of several variables;
- Find partial derivatives of multivariate functions
- Perform Marginal Analysis on multivariate functions
- Apply all rules of differentiation of multivariate functions correctly
- Confirm that Euler's Theorem has been satisfied

**Unit 9**: By the end of Unit 9, each student must be able to:

- Find stationary points of a multivariate function
- Classify the stationary points of a multivariate function

**Unit 10**: By the end of Unit 10, each student must be able to:

- Model a constrained optimization problem involving multivariate functions
- Solve a constrained optimization problem involving multivariate functions using Lagrange Multipliers
- Interpret the Lagrange Multipliers
- Solve a constrained optimization problem involving multivariate functions using Kuhn Tucker Conditions

# **General Objectives**

On successful completion of this course, students will be able to demonstrate that they have acquired the knowledge and skills of Mathematical Methods for Economics at the introductory level and thereby be in a position to logically approach situations at Level III in their undergraduate program that require the application of mathematical methods.

In addition, students will acquire a solid foundation for the mathematical analysis to be encountered in Microeconomics and Methods of Economic Investigation at the graduate level.

### **ASSESSMENT**

Assessment Objectives are linked to the Course Objectives. The approach to be adopted for assessment in this course has three (3) objectives:

- a. to effectively measure the students' proficiency in interpreting and using the mathematical concepts, symbols and terminology
- b. to effectively measure the students' proficiency in recognising the appropriate mix of mathematical concepts and methods that are required for addressing problems in the areas of economics, accounting and management
- c. to effectively measure the students' ability to apply the appropriate mix of mathematical methods in a logical manner.

Assessment will take the form of Coursework and a Final Examination.

The Coursework Component is comprised of a Diagnostic Exercise, Graded In-Class Tests, and Pre-Lecture Online Quizzes.

Each student is required to complete a **Diagnostic Activity**: this activity will provide students with an opportunity to revisit key concepts and methods captured in CXC CAPE Pure Mathematics or G.C.E. 'A' Level Mathematics or in ECON1004. There are **two** (2) **deliverables** for this diagnostic activity:

- 1. The submission of the solutions to the ECON 1004 Dec 2020 Final Examination Paper. Deadline for submission of the solutions on myelearning is the Tuesday of the second week of the semester.
- 2. Students will be provided with a soft copy of the Solutions to the Examination Paper via myelearning on the **Thursday of the second week of the semester**. On receipt of the solutions, students must review their submissions, undertake their own evaluation of their solutions as compared with mine, identify areas of weakness, develop their own strategies for addressing those weaknesses, and write a concise summary of the weaknesses identified and the corrective strategy. **Deadline for submission of the summary on myelearning is Sunday 30**th **January.**

Marks will be awarded only on submission of the two deliverables.

Students will be continuously assessed by way of at least three (3) **In-Class Tests** which will be administered at approximately **fortnightly** intervals beginning with **Week #4**. The questions that comprise each test will be based on the topics covered in the lectures over the previous two weeks and the tutorial assignment(s). Solutions to each in-class test will be posted on the course website.

Students must be prepared for at most three (3) **online quizzes** to be posted on Myelearning during Week #5, 8 & 10 of the semester.

Students will be required to engage Lecturers and Tutors by way of Office Hours Consultation <u>consistently</u> over the semester in discussion on concepts and approaches to problem solving. Experience has shown that students, who are so engaged, perform well.

Students are strongly advised to familiarize themselves during Week 1 of the Semester with the University Regulations on Examination Irregularities particularly in so far as these regulations relate to Cheating during coursework assessment activities and/or the final examination. The Lecturers will apply these regulations to students determined to have cheated during any of the coursework activities.

The **Final Examination** at the end of the Semester will be based on the entire course. Students are strongly advised to use the Learning Outcomes of the course as a meter for measuring their preparation for the final examination. The examination will be of two-hour duration. All questions will be compulsory.

The **Overall Mark** in the course will therefore be a composite of the marks obtained in the coursework and final examination components; the relative weights being:

The **coursework marks** will be allocated as follows:

Diagnostic Activity	3%
Homework submission, class participation	2%
Pre-Lecture Online Quizzes	10%
In-Class Tests	25%.

The **final examination** at the end of the semester will consist of a two (2) hour paper, comprising four (4) questions drawn from all units of the course. Students will be required to answer all four (4) questions.

The **overall mark** for each student will be a weighted score of the coursework and final examination marks; the weights being

Coursework 40% Final Examination 60%.

### **TEACHING STRATEGIES**

The course will be delivered by way of an individual diagnostic activity, lectures, class discussion, tutorials, in-tutorial presentations, pre-lecture online quizzes, in-class tests, in-class group presentation, and consultation during office hours or by appointment.

Seven (7) **Assignments** will be issued during the course. These assignments must be completed at a pace that fits into the schedule of In-Class Tests.

Tutorial Assignment	Related Units
1	Part A – Unit 1; Part B – Unit 2
2	Part A – Unit 3; Part B – Unit 4
3	Unit 5
4	Unit 6
5	Unit 7
6	Unit 8
7	Unit 9

Self-assessment/diagnosis at the start of the course will be encouraged and should not be underestimated. In this regard, students reading the course for the first time must (a) complete all questions in the provided Examination Paper for ECON1004 (b) compare their solutions with the Mark Scheme for the examination paper (c) identify and report on their knowledge/skill gaps and their own plan to close these gaps.

Participation in class discussion is a critical input to the feedback process within a lecture. The rules of engagement for these discussions will be defined by the Course Lecturer at the first lecture.

Pre-Lecture Online Quizzes and In-Class Tests will be administered by the Course Lecturer. These are aimed at assisting the student to (a) become familiar with the key concepts to be discussed in a new unit of the course and (b) measure the extent to which the learning outcomes for a previous unit has been derived.

Students will be provided with three (3) contact hours weekly; two (2) for lectures and one (1) for tutorials.

Registration for tutorial classes will be online at the end of Week #1.

In addition, the Course Lecturers will be available for consultations during specified **Office Hours** and at other times by appointment.

Attendance at <u>all</u> Lectures and Tutorial Classes will be treated as **compulsory**. **University Regulation #19** allows for the Course Lecturer to debar from the Final Examination students who do not attend at least 75% of tutorials. The Course Lecturers will be enforcing this regulation.

# **Course Schedule**

Week	Activity
1	Diagnostic Activity; Orientation Lecture; Unit 1 Lecture
17 <sup>th</sup> Jan.	
2	Unit 1 Lecture;
24 <sup>th</sup> Jan	
3	Unit 2 Lecture; Tutorial;
31 <sup>th</sup> Jan	
4	Unit 3 Lecture; Tutorial; Consultation during Office Hours;
7 <sup>th</sup> Feb	
5	Unit 4 Lecture; Tutorial; In-Course Test I
14 <sup>th</sup> Feb	
6	Unit 4 Lecture; Tutorial
21 <sup>st</sup> Feb	
7	Unit 5 Lecture; Tutorial; Consultation during Office Hours;
28 <sup>th</sup> Feb	
8	Unit 6 Lecture; Tutorial; Pre-Lecture Online Quiz I
7 <sup>th</sup> Mar	
9	Unit 7 Lecture; Tutorial; Consultation during Office Hours;
14 <sup>th</sup> Mar	
10	Unit 8 - 9 Lecture; Tutorial; Consultation during Office Hours; In-Course Test
21 <sup>st</sup> Mar	II
11	Unit 10 Lecture; Tutorial; Consultation during Office Hours; Pre-Lecture
28 <sup>th</sup> Mar	Online Quiz II
12	Unit 10 Lecture; Tutorial; Consultation during Office Hours
4 <sup>th</sup> Apr	
13	Course Review; Tutorial; Consultation during Office Hours;
11 <sup>th</sup> Apr	

### **REFERENCE TEXTS**

- 1. **A.C. Chaing & K. Wainwright**: Fundamental Methods of Mathematical Economics, Fourth Edition, Mc Graw-Hill/Irwin, New York. 2005
- 2. **Dowling, Edward T.**, <u>Calculus for Business, Economics, and the Social Sciences,</u> Schaum's Outline Series, McGraw-Hill.
- 3. Hoffman, L. D. Calculus for Business, Economics, and the Social Sciences, McGraw-Hill.
- 4. **Ayres, Frank** Calculus, 2nd Edition, New York, McGraw-Hill, 1964
- 5. **Lewis J Parry** An Introduction to Mathematics for Students of Economics. Macmillan 1970
- 6. **Haeussler, E., Paul, R. and Wood, R**., <u>Introductory Mathematical Analysis for Business, Economics and the Life and Social Sciences</u>, Eleventh Edition Prentice Hall. 2005
- 7. **Tan, S. T.**, College Mathematics for the Managerial, Life and Social Sciences, Sixth Edition, Thomson Brooks/Cole. 2005

#### ADDITIONAL INFORMATION

- "Any candidate who has been absent from the University for a prolonged period during the teaching of a particular course for any reason other than illness or whose attendance at prescribed lectures, classes, ... tutorials, ... has been unsatisfactory or who has failed to submit essays or other exercises set by his/her teachers, may be debarred by the relevant Academic Board, on the recommendation of the relevant Faculty Board, from taking any University examinations. The procedures to be used shall be prescribed in Faculty Regulations."
- "97 (i) Cheating shall constitute a major offence under these regulations.
  - (ii) Cheating is any attempt to benefit one's self or another by deceit or fraud.
  - (iii Plagiarism is a form of cheating.
  - (iv) Plagiarism is the unauthorized and/ or unacknowledged use of another person's intellectual effort and creations howsoever recorded, including whether formally published or in manuscript or in typescript or other printed or electronically presented form and includes taking passages, ideas or structures from another work or author without proper and unequivocal attribution of such source(s), using the conventions for attributions or citing used in this University.
- 103 (i) If any candidate is suspected of cheating, or attempting to cheat, the circumstances shall be reported in writing to the Campus Registrar.

The Campus Registrar shall refer the matter to the Chairman of the Campus Committee on Examinations. If the Chairman so decides, the Committee shall invite the candidate for an interview and shall conduct an investigation. If the candidate is found guilty of cheating or attempting to cheat, the Committee shall disqualify the candidate from the examination in the course concerned, and may also disqualify him/her from all examinations taken in that examination session; and may also disqualify him/her from all further examinations of the University, for any period of time, and may impose a fine not exceeding Bds\$300.00 or J\$5000.00 or TT\$900.00 or US\$150.00 (according to campus). If the candidate fails to attend and does not offer a satisfactory excuse prior to the hearing, the Committee may hear the case in the candidate's absence."

Grading Sys	Grading System		
2016/2017 Grading Policy			
Grade	<b>Quality Points</b>	Mark%	
A+	4.3	90-100	
Α	4.0	80-89	
Α-	3.7	75-79	
B+	3.3	70-74	
В	3.0	65-69	
B-	2.7	60-64	
C+	2.3	55-59	
С	2.0	50-54	
F1	1.7	45-49	
F2	1.3	40-44	
F3	0.0	0-39	

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